



Investigation on the non-Darcy term in flow equations

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**SPE HUN Workshop
Visegrád, 16 November 2017**

Society of Petroleum Engineers

Agenda

- Darcy's equation
- Modification of Darcy's law
- Steps of the research
- Grouping & classing
- Sensitivity tests for oil and gas
- Behaviour of the β factor under changing PVT properties
- Summary table and how to use it

Darcy's equation

$$q_o = \frac{(P_e - P_{wf}) \times (k_o \times h)}{141.2 \times \mu_o B_o \left[\ln \left(0.472 \left\{ \frac{r_e}{r_w} \right\} \right) \right]}$$

$$q_g = \frac{(P_e^2 - P_{wf}^2) \times (k_g \times h)}{1.424 \times 10^3 \mu_g T z \left[\ln \left(0.472 \left\{ \frac{r_e}{r_w} \right\} \right) \right]}$$

Equation for normal fluid flow through porous medium

Neglected forces in case of low fluid velocities

Capillary force

Inertial forces

Turbulent friction force

Significant forces in case of high fluid velocities

Compression force

Gravitational force

Capillary force

Inertial forces

Turbulent friction force

Modification of Darcy's law

The equation of Forseheimer (1901)

$$-\frac{dP}{dL} = \mu \frac{v}{k} + av^2$$

The equation of Jones (1967)

For oil wells

For gas wells

$$P_e - P_{wf} = Aq_o^2 + Bq_o$$

$$A = \frac{2.30 \times 10^{-14} \times \beta B_o^2 \rho}{h^2 r_w}$$

$$B = \frac{141.2 \times \mu_o B_o \left[\ln \left(0.472 \left\{ \frac{r_e}{r_w} \right\} \right) \right]}{k_o h}$$

$$P_e^2 - P_{wf}^2 = Aq_g^2 + Bq_g$$

$$A = \frac{3.16 \times 10^{-12} \times \beta \gamma_g Tz}{h^2 r_w}$$

$$B = \frac{1.424 \times 10^3 \mu_g Tz \left[\ln \left(0.472 \left\{ \frac{r_e}{r_w} \right\} \right) \right]}{k_g h}$$

β factor:
dominant role in
the flow of the
fluids

The β factor

- inherited from the equation of Forchheimer
- causes the differences from the Darcy equation
- literature \longrightarrow lot of formula for the beta factor

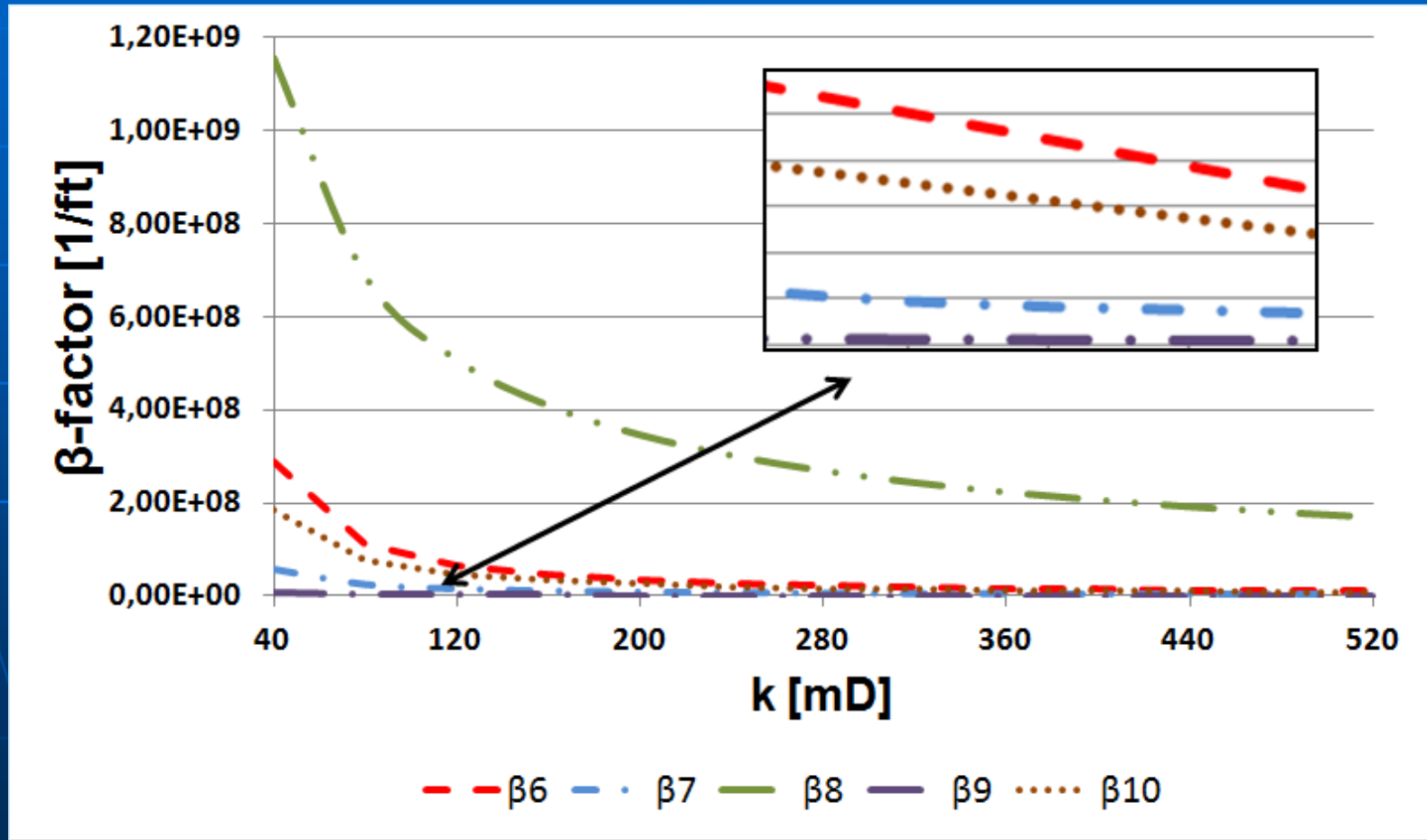
Examples for the investigated β factors

<i>Authors</i>	Geertsma (1974)	Pascal (1980)	Cole & Hartman (1998)
<i>Equations</i>	$\left(\frac{0.005}{\Phi^{5.5} k^{0.5}} \right)$	$\left(\frac{4.8 \times 10^{12}}{k^{1.176}} \right)$	$\frac{8.17 \times 10^9 \Phi^{0.537}}{k^{1.79}}$

The steps of our investigation

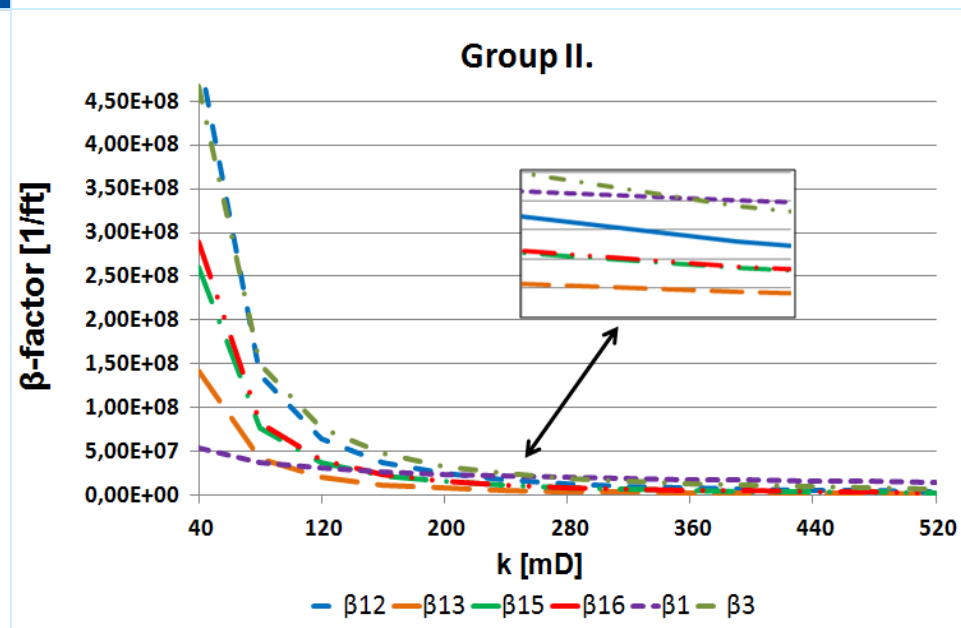
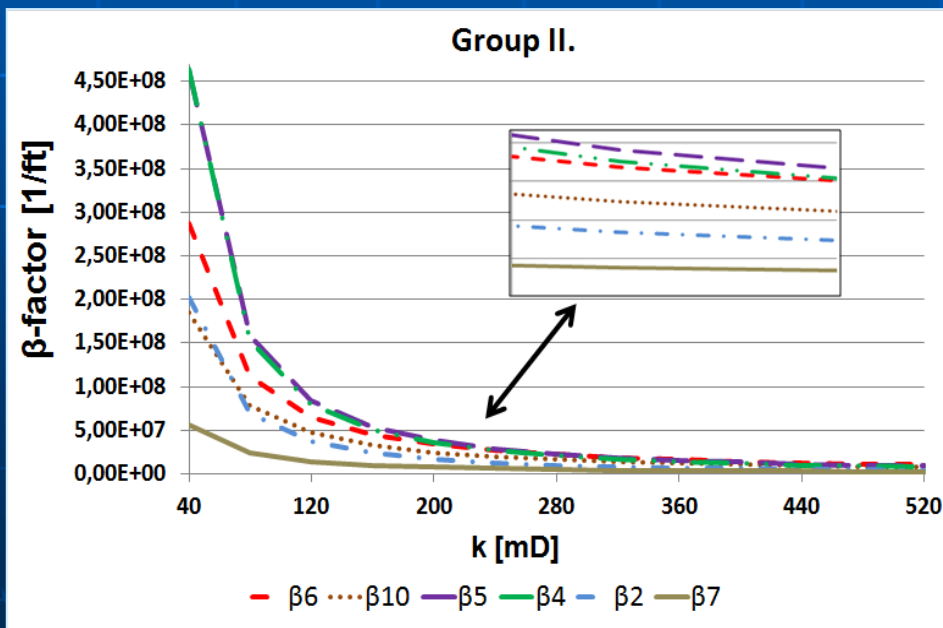
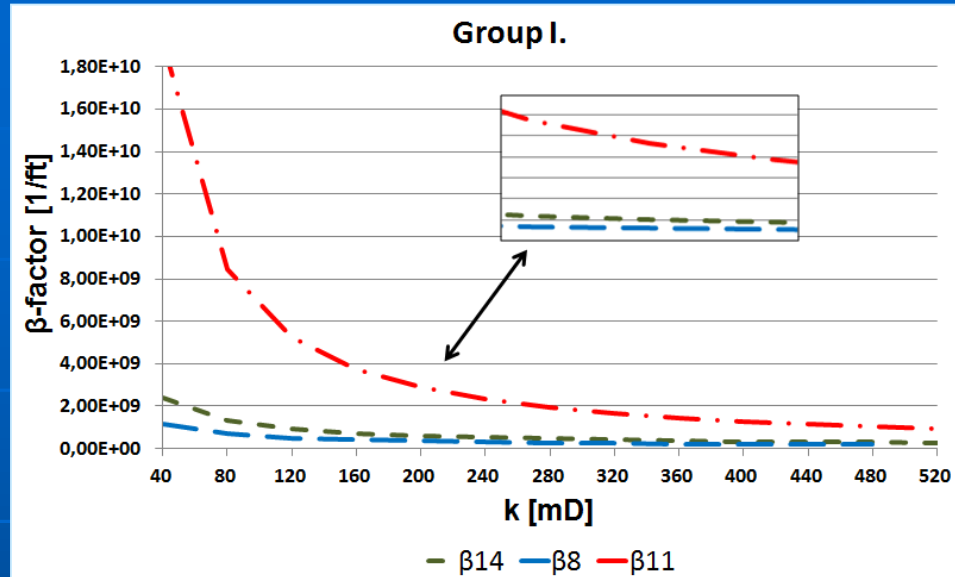
- I. Grouping & classing based on similar trends of the curves
- II. Sensitivity analysis for oil and gas wells – individual properties
- III. Sensitivity analysis for oil and gas wells – based on depth

Significant differences between the 20 β equations



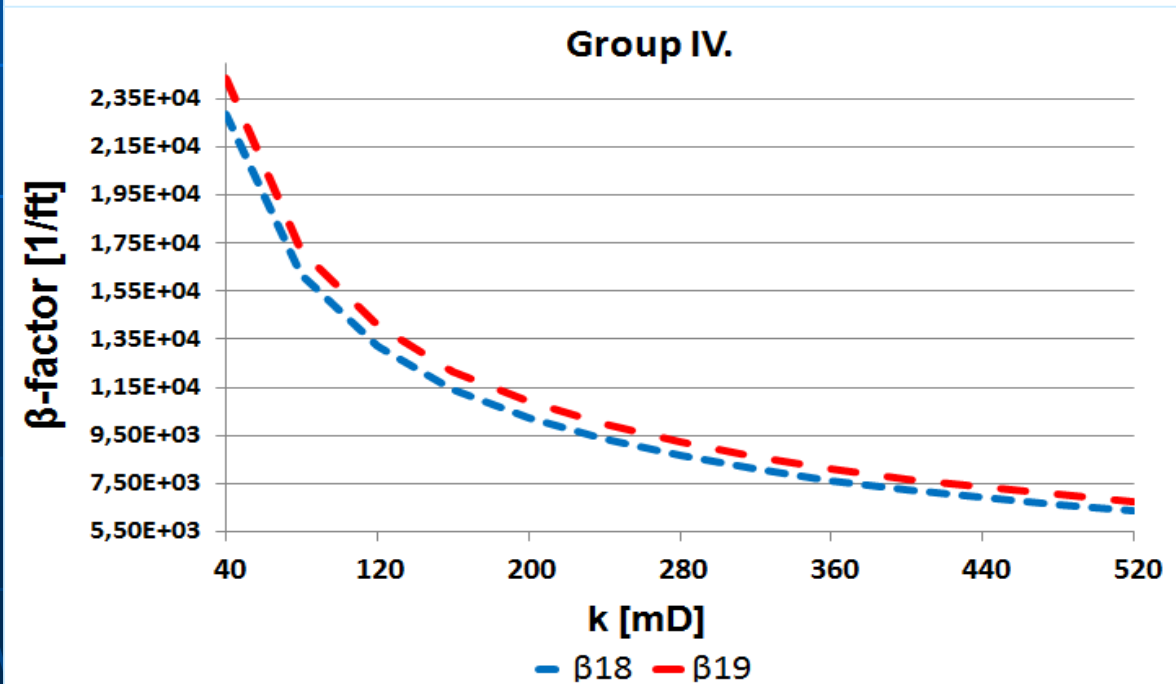
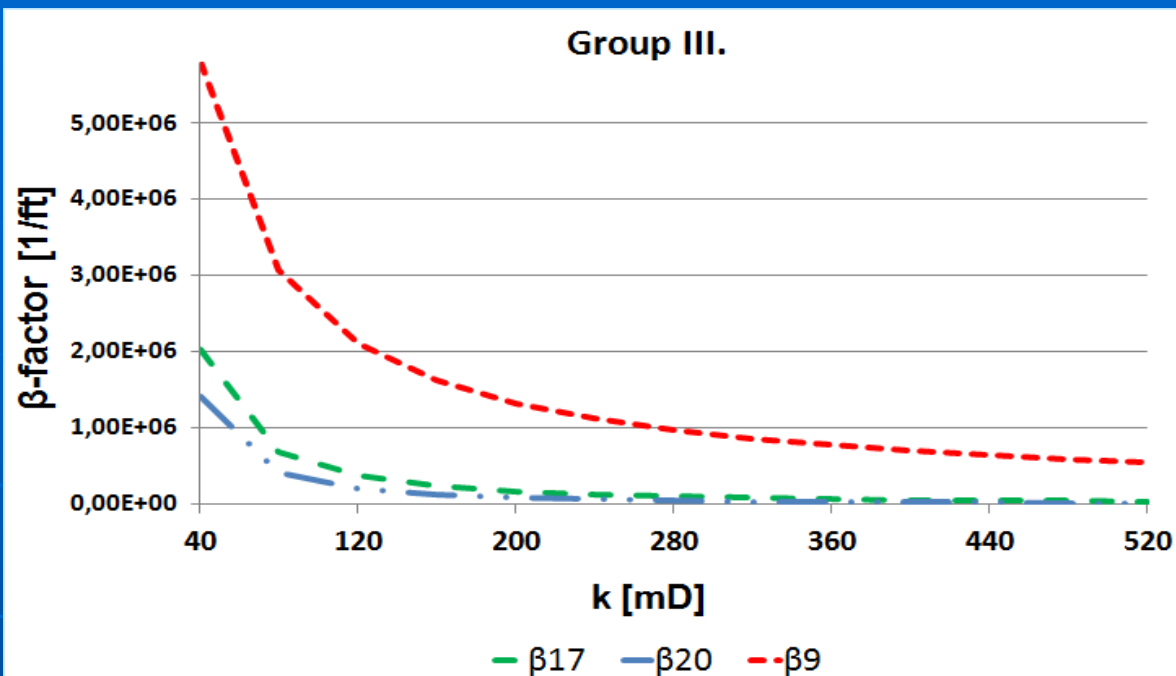
4 Groups

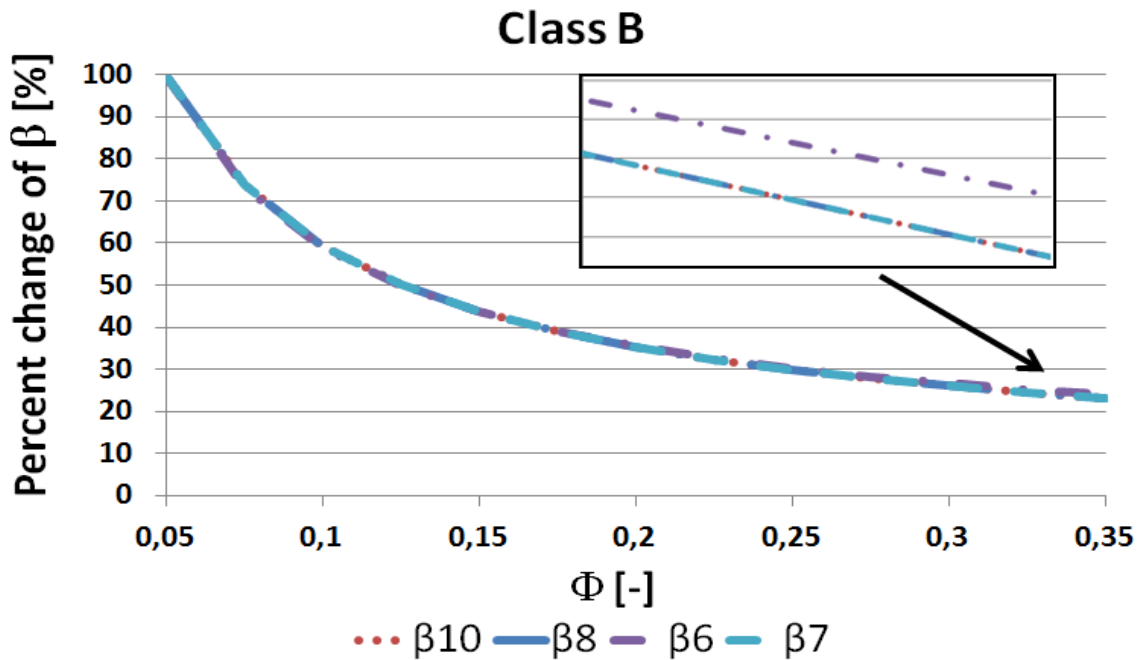
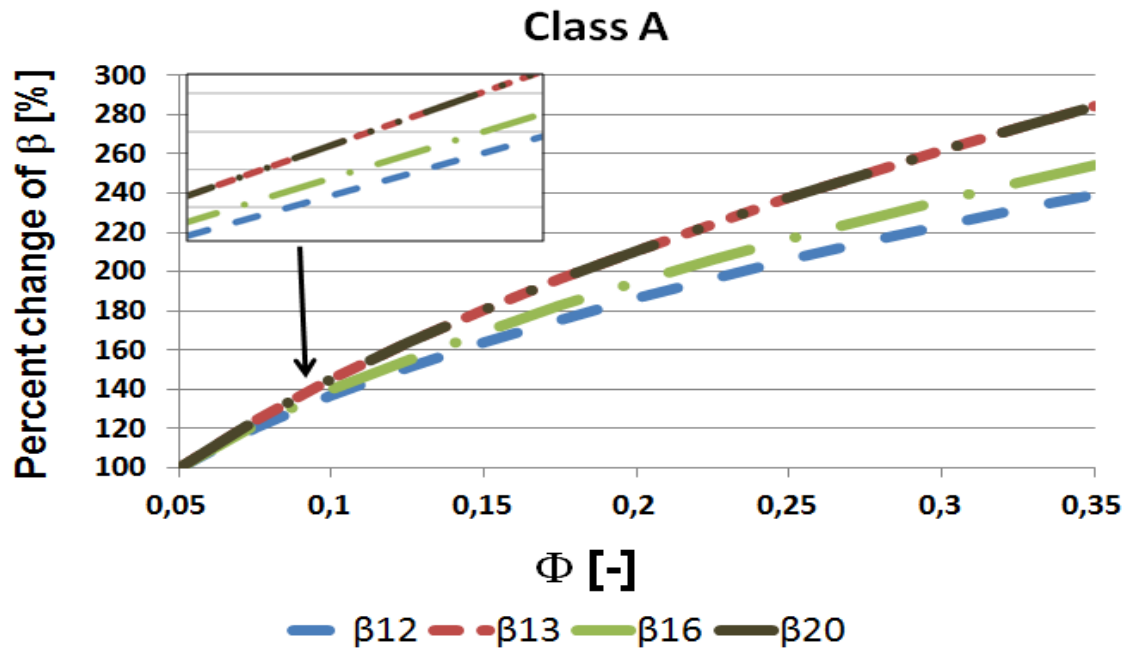
- Group I.
- Group II.



4 Groups

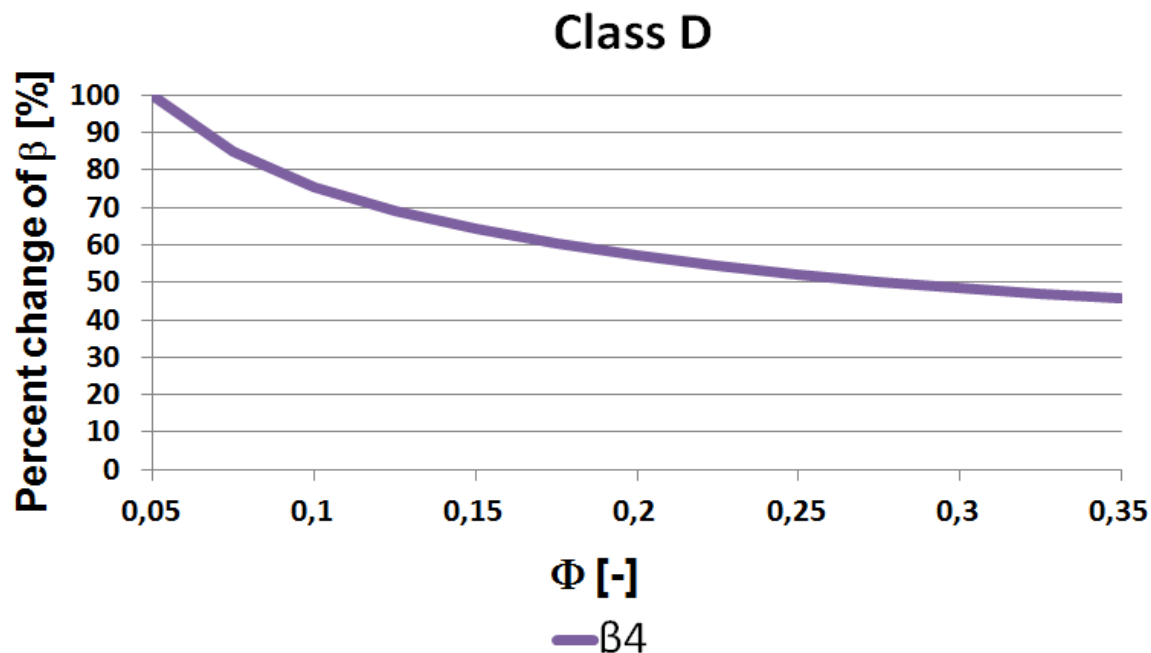
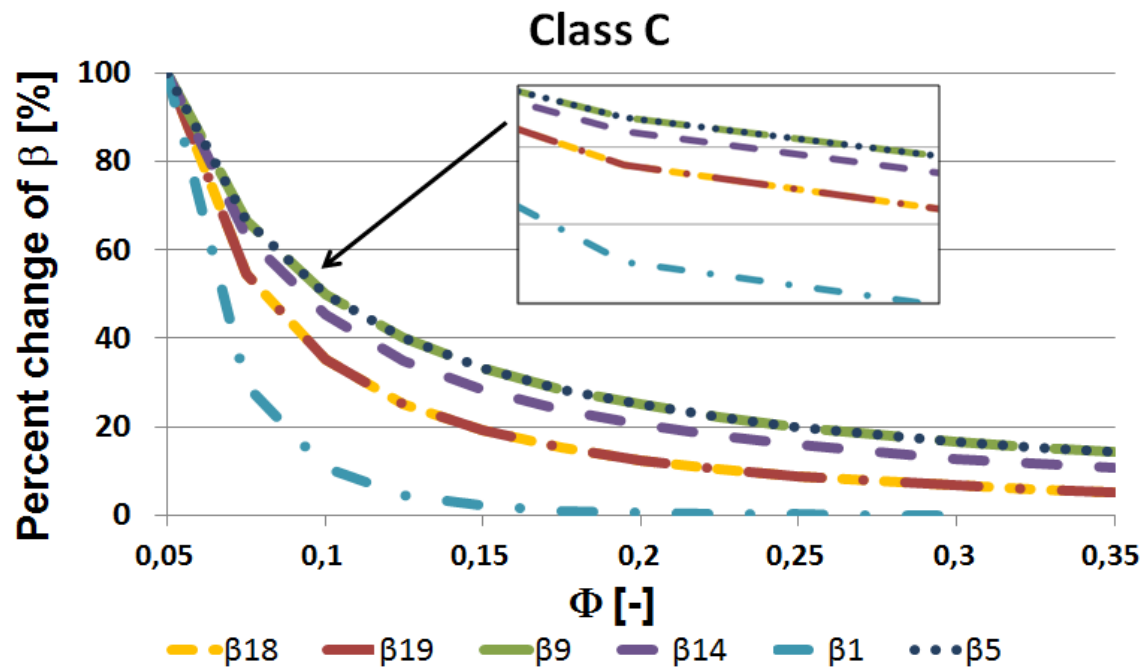
- Group III.
- Group IV.





5 Classes

- Class A
- Class B



5 Classes

- Class C
- Class D

+ Class E

Sensitivity analyzes

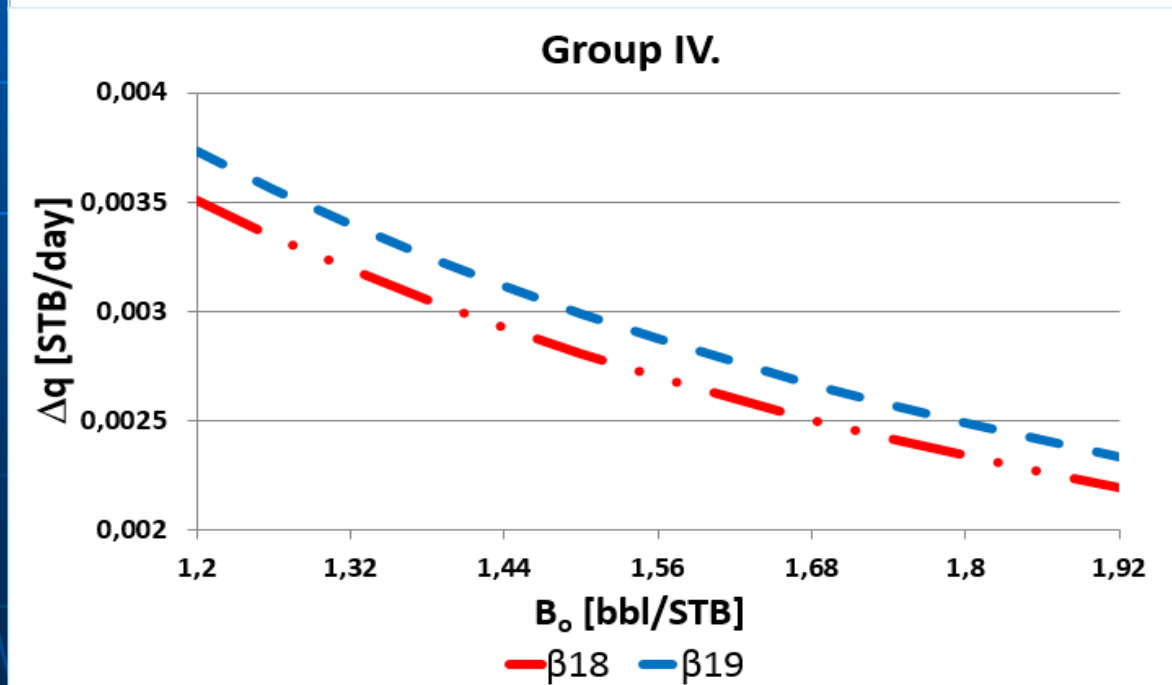
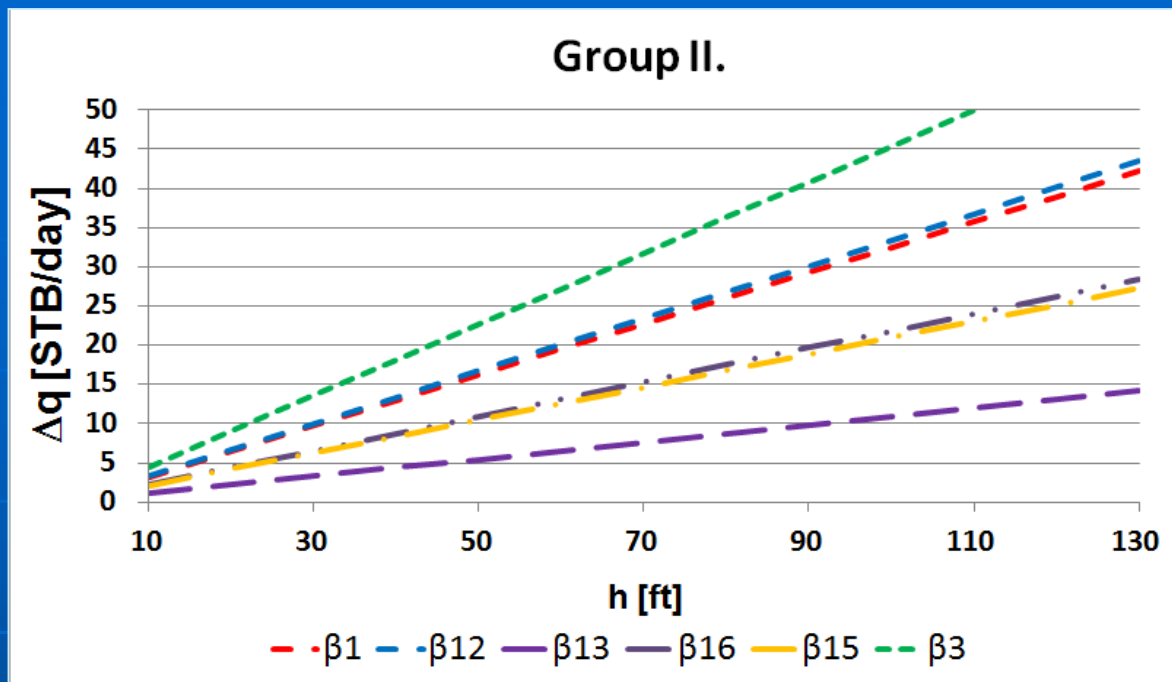
In case of oil:

- Permeability(k)
- Viscosity(μ)
- Formation volume factor(B_o)
- Reservoir thickness(h)

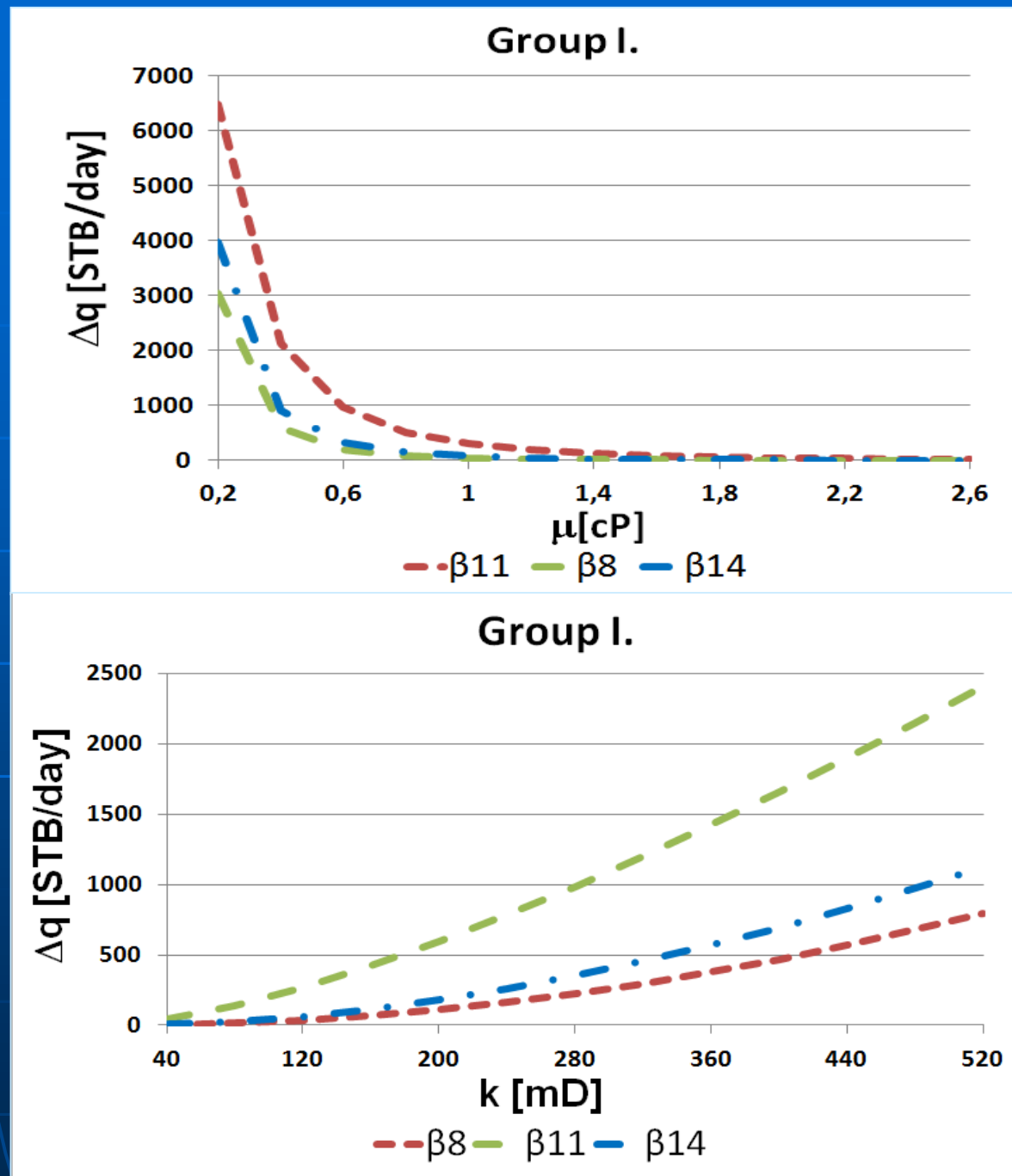
In case of gas:

- Permeability(k)
- Viscosity(μ)

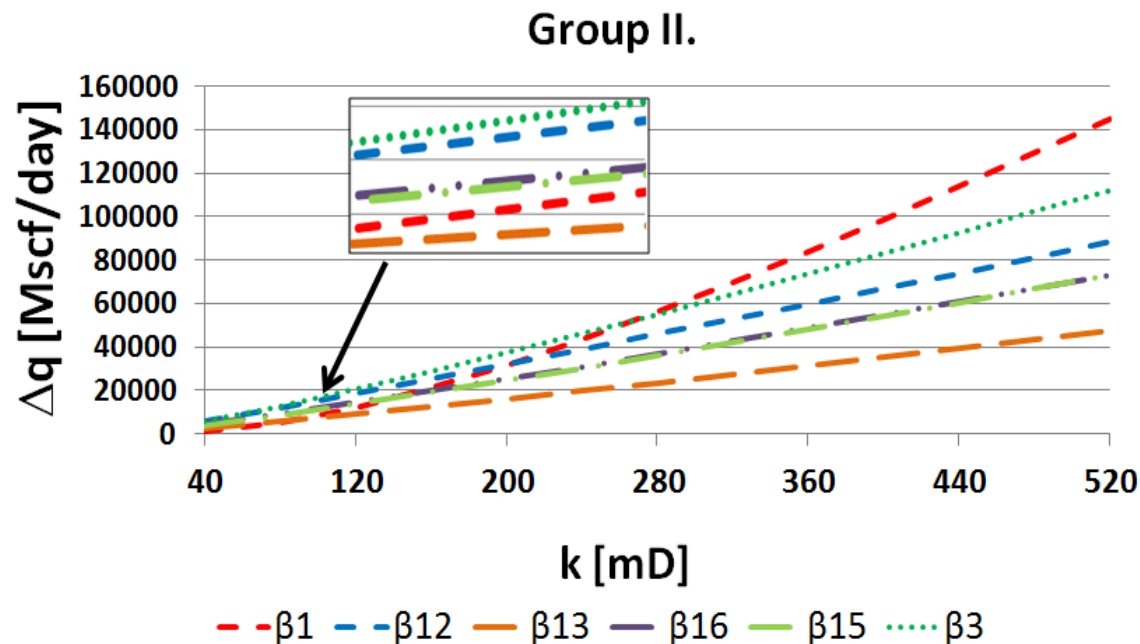
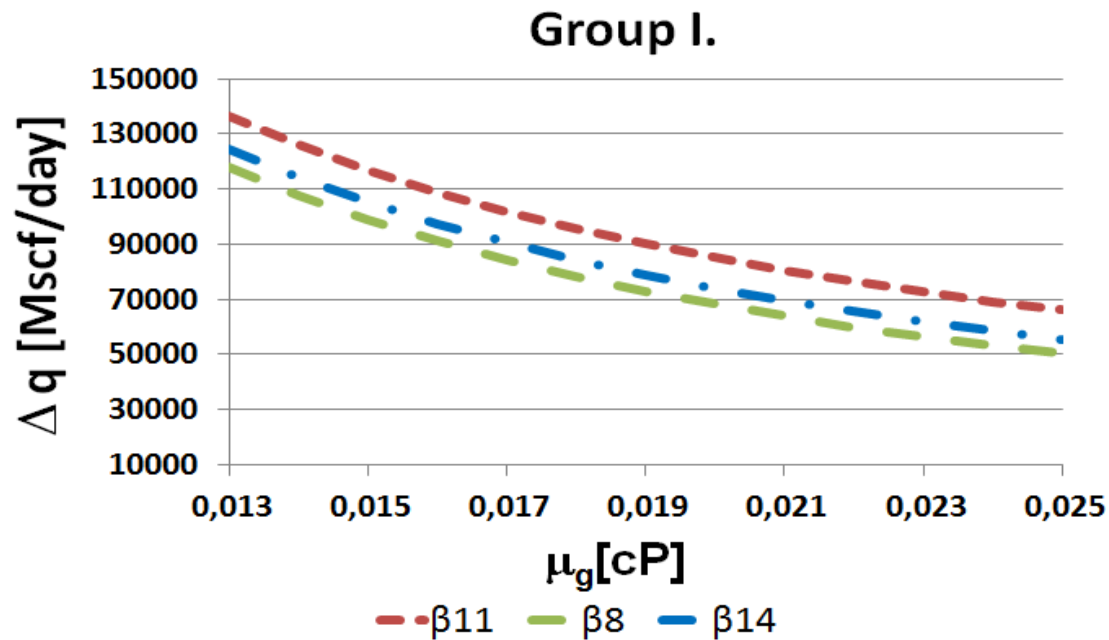
Sensitivity analyzes for OIL



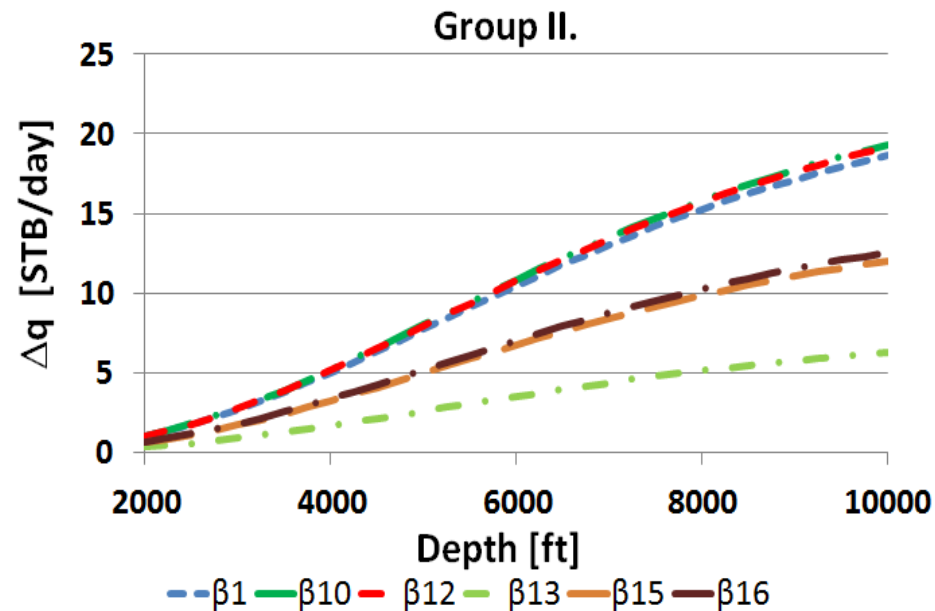
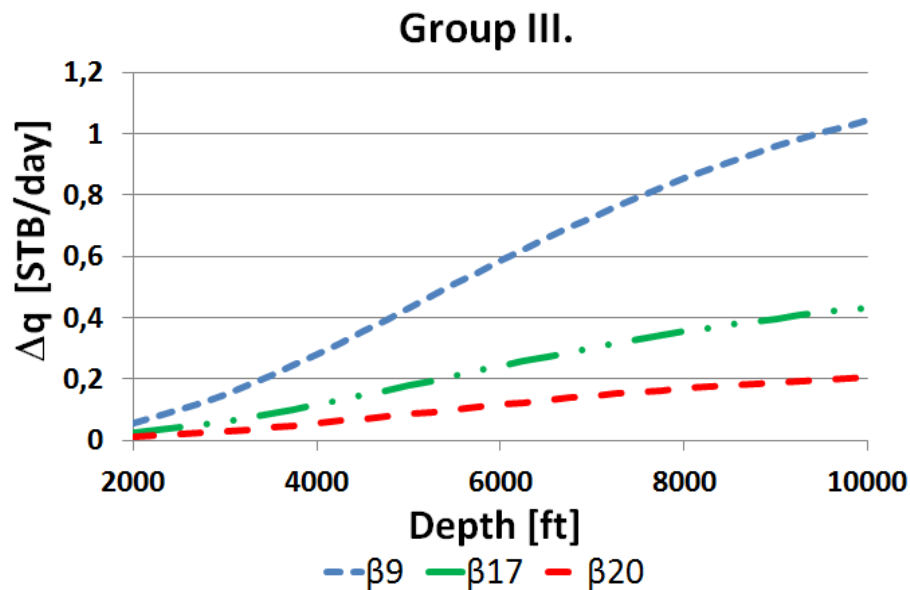
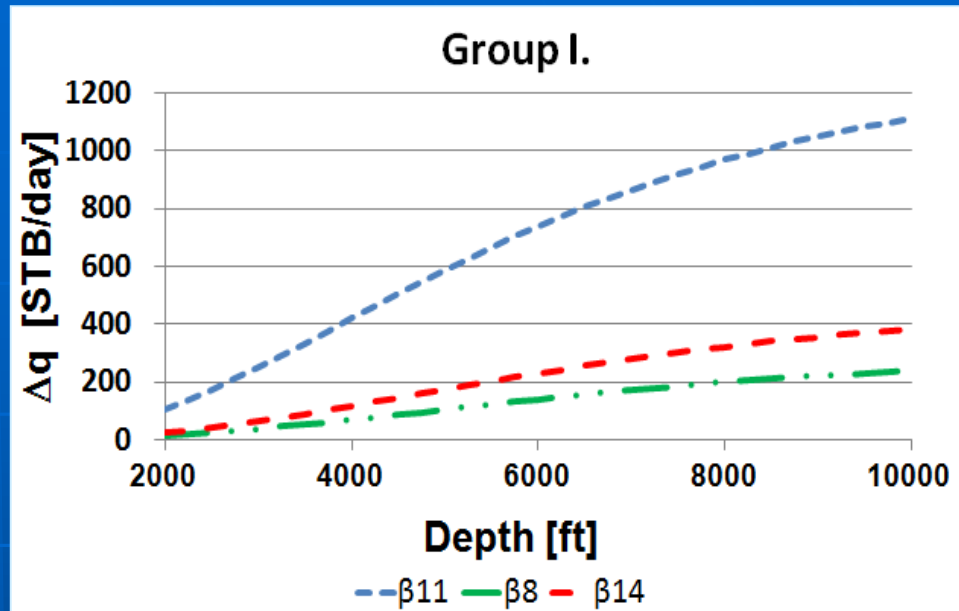
Sensitivity analyzes for OIL



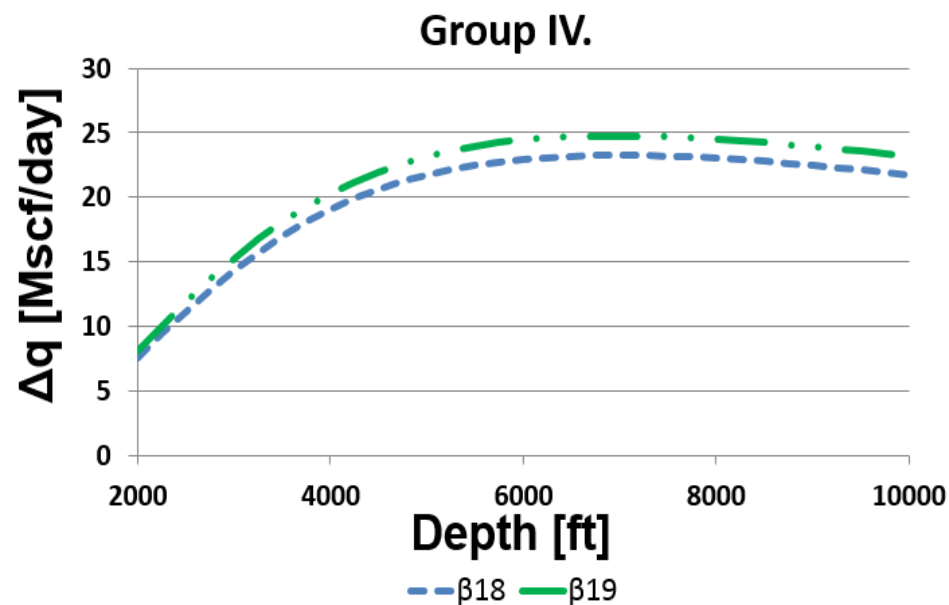
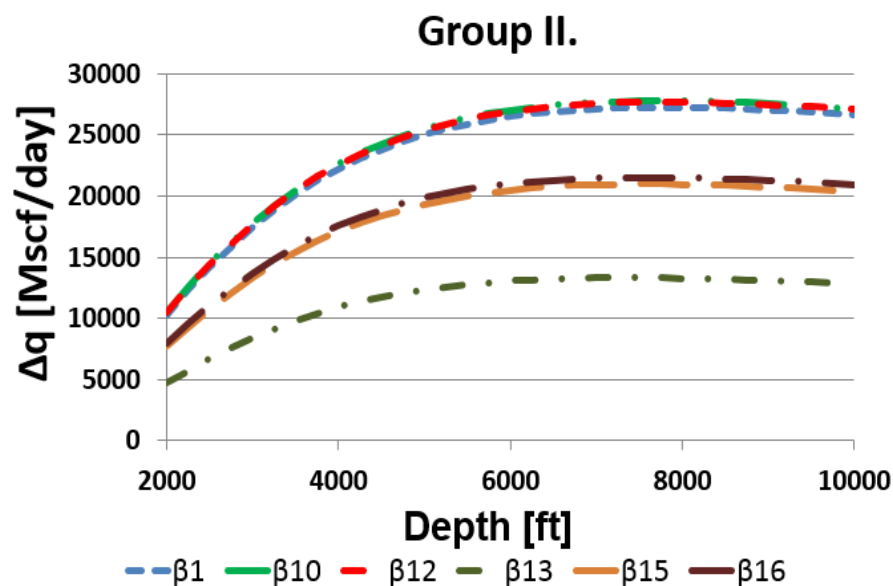
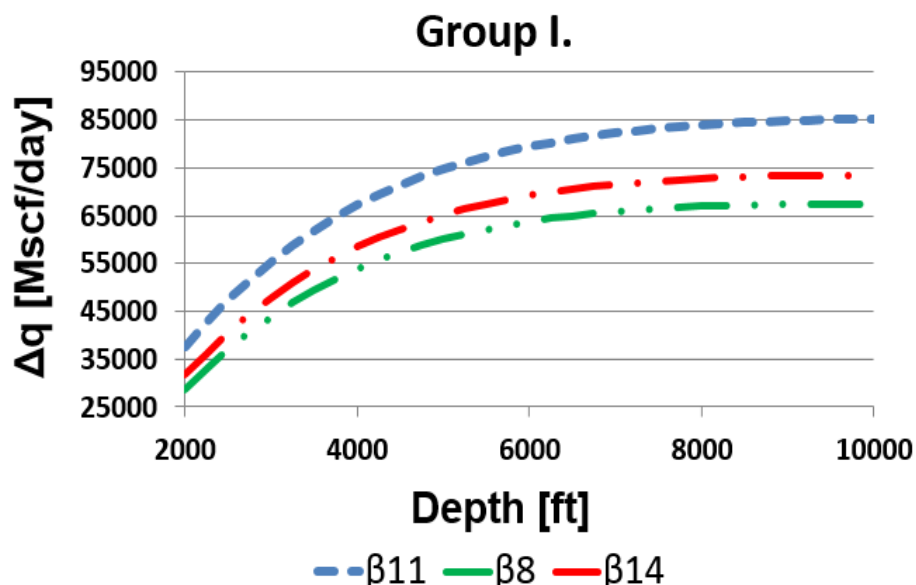
Sensitivity analyzes for GAS



Sensitivity analyzes based on the depth for OIL



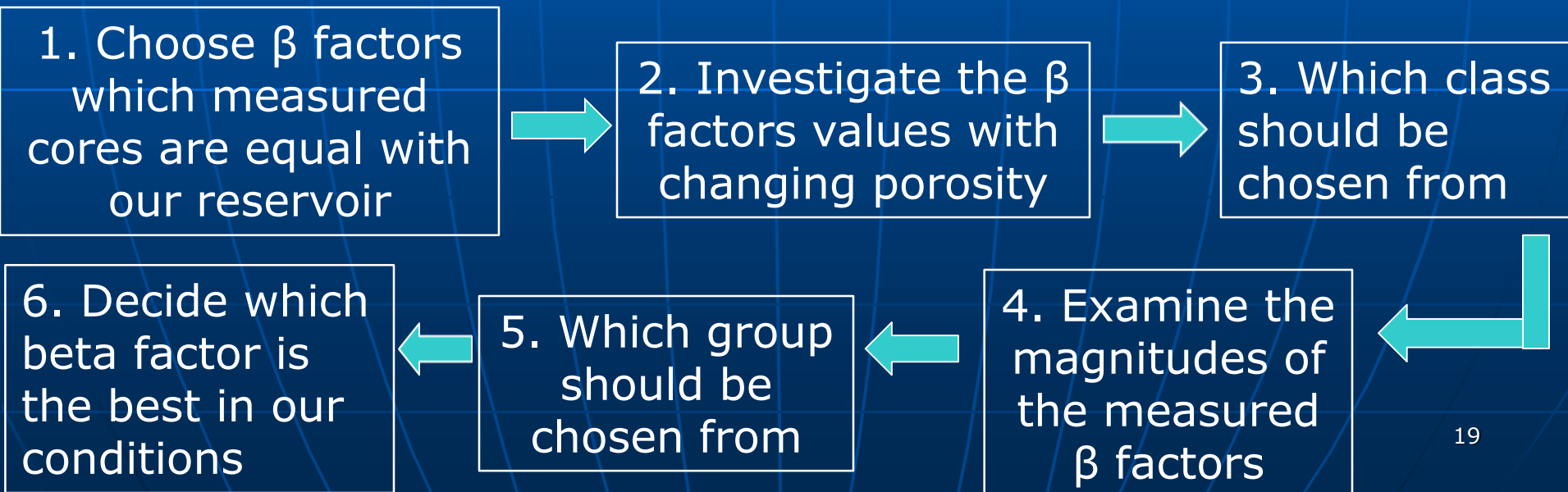
Sensitivity analyzes based on the depth for GAS



β factor	Formula	Measurement	Group	Class
β_1	$\beta_1 = \left(\frac{0.005}{\phi^{2.3} k^{0.2} \times 10^{-11}} \right) \times 30.5$	sandstone	II.	C
β_2	$\beta_2 = 6.15 \times 10^{10} (k)^{-1.22}$	sandstone limestone	II.	E
β_3	$\beta_3 = 1.98 \times 10^{11} (k)^{-1.44}$	sandstone limestone	II.	E
β_4	$\beta_4 = 7.89 \times 10^{10} (k)^{-1.42} [\phi(1 - S_w)]^{-0.404}$	sandstone limestone	II.	D
β_5	$\beta_5 = 2.11 \times 10^{10} (k)^{-1.22} [\phi(1 - S_w)]^{-1.0}$	sandstone limestone	II.	C
β_6	$\beta_6 = \frac{1}{[\phi(1 - S_w)]^2} \times e^{42 - \sqrt{427 + 21 - \ln(\phi/(2(1 - S_w)))}}$	sandstone limestone	II.	B
β_7	$\beta_7 = \frac{5.5 \times 10^9}{k^{1.22} \phi^{0.72}} \times 0.305$	sandstone limestone	II.	B
β_8	$\beta_8 = \frac{5.5 \times 10^9}{k^{2/3} \phi^{2/3}}$	Wilcox-homok	I.	B
β_9	$\beta_9 = \left(\frac{5.123 \times 10^{-2}}{\phi} \left[\frac{1}{(1 - S_w)\sqrt{k \times 10^{-11}}} \right]^{1.229} \right) \times 30.5$	sandstone	III.	C
β_{10}	$\beta_{10} = (1.82 \times 10^8 k^{-2/3} \phi^{-2/3}) \times 30.5$	sandstone limestone dolomite	II.	B
β_{11}	$\beta_{11} = \left(\frac{4.8 \times 10^{11}}{k^{1.170}} \right) \times 0.305$	Low permeability hydraulically fractured well's data	I.	E
β_{12}	$\beta_{12} = \frac{1.07 \times 10^{12} \times \phi^{0.469}}{k^{1.88}}$	sandstone limestone	II.	A
β_{13}	$\beta_{13} = \frac{2.49 \times 10^{11} \phi^{0.287}}{k^{1.79}}$	sandstone limestone	II.	A
β_{14}	$\beta_{14} = \frac{9 \times 10^9}{k^{0.7} \times \phi^{0.7}}$	sandstone	I.	C
β_{15}	$\beta_{15} = \frac{17.2 \times 10^{10}}{k^{1.70}}$	sandstone	II.	E
β_{16}	$\beta_{16} = \frac{4.8 \times 10^{11}}{k^{1.8} \times \phi^{-0.48}}$	sandstone	II.	A
β_{17}	$\beta_{17} = \frac{2.018 \times 10^9}{k^{1.20}} \times 0.305$	limestone, crystal limestone, well-classed sandstone	III.	E
β_{18}	$\beta_{18} = \frac{1}{\phi} \sqrt{\frac{1.8 \times 10^9}{k \phi}} \times 0.305$	sandstone	IV.	C
β_{19}	$\beta_{19} = \frac{1}{\phi} \sqrt{\frac{245 \times 10^8}{12k \phi}} \times 0.305$	sandstone	IV.	C
β_{20}	$\beta_{20} = \frac{8.17 \times 10^9 \phi^{0.287}}{k^{1.79}} \times 0.305$	sandstone limestone	III.	A

Results of the research

β factor	Formula	Measurement	Group	Class
β ₁	$\beta_1 = \left(\frac{0.005}{\phi^{5.5} k^{0.5} \times 10^{-11}} \right) \times 30.5$	sandstone	II.	C
β ₂	$\beta_2 = 6.15 \times 10^{10} (k)^{-1.55}$	sandstone limestone	II.	E
β ₃	$\beta_3 = 1.98 \times 10^{11} (k)^{-1.64}$	sandstone limestone	II.	E



References:

1. A. B. H., R. A. K., M. N. A., D. B. S. és R. I. M., „Numerical and Experimental Modeling of Non-Darcy Flow in Porous Media,” SPE, Trinidad, West Indies, 2003.
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Thanks for your attention!



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SPE Student Chapter



Hungarian Section